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# Structure and energetics of small iron clusters

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Abstract Electronic properties of Fe<sub>2-10</sub> clusters and their ions are described by an all-electron ab initio density functional theory computational analysis using the Handy's OPTX exchange and the gradient-corrected correlation functional of Perdew, Burke and Ernzerhof with a triple-zeta valence basis set plus polarization functions. Ground state structures, magnetic moments, dissociation energies, binding energies, IR vibrational spectra, vertical and adiabatic ionization energies, and electron affinities are reported. Two possible states for Fe<sub>2</sub> which are separated by 81.54 meV are described as possible Fe<sub>2</sub>, while the septet (ground state) yields an accurate bond distance (error of 0.02 Å); the nonet yields a precise vibrational frequency (error of 10.1 cm<sup>-1</sup>). Fe<sub>2</sub> binding energy (0.05 eV/atom error) more closely resembles experimental data than any other previously reported computational methods. In addition, the Fe<sub>6</sub> is found to be the most stable cluster within our set being analyzed.

Keywords Ab initio · DFT · Iron cluster · OPBE · TZV

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#### Introduction

Because of its physical properties, iron is one of the most important ferromagnetic materials among the first-row transition metals (TM). Its high magnetic moments as well as its high values of transverse relaxativity make iron and its oxides a suitable ingredient in magnetic nanoparticles (MNPs). High values of transverse relaxativity are caused by an external magnetic field and facilitate the detection of signals by means of the iron transverse relaxation. MNP-based devices are employed in applications such as biosensing using magnetic resonance [1], detecting tuberculosis bacteria [2], and for magnetic enrichment in *in vivo* detection of circulating tumor cells [3].

From a cluster physics viewpoint, it is difficult to perform an accurate study of iron clusters at empirical and ab initio levels [4, 5]; nevertheless, density functional theory (DFT) has been successfully applied and become popular for computation of TM properties in the last decades [6]. The capability of DFT to consider static correlation allows us to find the correct electronic structure among several low lying states [5], thereby leading us to obtain the correct magnetic and structural properties. Thus, the presence of a strong correlation in partially filled d orbitals leads to the highest magnetic moments. Previous computational studies for small iron clusters [7-16] have shown a size-dependence and a larger effective magnetic moment per atom over the bulk value of  $2.22\mu_{\rm B}$ ; this value is approached experimentally for more than 500 atoms [17]. While iron cluster structures resulted in distorted geometries far away from the crystalline bcc bulk structure, these distortions are predicted by the Jahn-Teller effect [18].



Fig. 1 Optimized structures, relative energies and multiplicities (M) for the Fe<sub>n</sub> (n=2-10) lowest conformation found for the ground states (labeled with **a**) and some isomers (labeled **b** with and/or **c**), including an excited state for Fe<sub>10</sub>

In this work we emphasize the quality of all-electron calculations in the framework of DFT for finding the most stable  $Fe_n$  clusters. In addition, we also calculate the iron

cluster ions for a deeper understanding of the stability of neutral clusters. Optimized structures are obtained from unconstrained symmetries using the OPBE/TZV level of

**Table 1** Optimized distances  $(d_{mp})$  between atoms *m* and *p* for the Fe<sub>n=2-10</sub> ground states shown in Fig. 1

n	<i>d</i> <sub>12</sub>	<i>d</i> <sub>23</sub>	<i>d</i> <sub>34</sub>	<i>d</i> <sub>45</sub>	<i>d</i> <sub>56</sub>	<i>d</i> <sub>67</sub>	$d_{78}$	<i>d</i> <sub>89</sub>	<i>d</i> <sub>9(10)</sub>
2	2.003								
3	2.167								
	2.283	2.282							
4	2.239								
	2.566	2.239							
	2.239	2.566	2.239						
5	2.668								
	2.264	2.263							
	2.298	2.299	2.384						
	2.298	2.298	2.382	3.688					
6	2.284								
	2.553	2.285							
	2.284	2.799	2.285						
	3.611	2.284	2.554	2.284					
	2.552	2.283	3.611	2.283	2.553				
7	2.295								
	2.534	2.316							
	2.274	3.656	2.257						
	2.534	3.793	3.678	2.256					
	2.295	2.453	3.793	3.656	2.316				
	2.704	2.331	2.315	2.600	2.315	2.332			
8	2.814								
	2.502	2.501							
	2.239	2.239	2.287						
	2.502	2.501	3.401	3.809					
	2.239	2.239	3.809	2.729	2.286				
	2.278	3.412	2.321	3.792	2.320	3.792			
	3.414	2.278	2.321	3.793	2.321	3.793	2.294		
9	2.424								
	2.632	2.334							
	2.425	3.669	2.334						
	2.311	3.767	3.887	2.355					
	2.312	2.355	3.888	3.768	2.356				
	2.631	2.333	2.481	2.334	2.338	2.338			
	2.312	2.355	2.339	3.768	4.544	3.887	3.887		
	2.311	3.766	2.338	2.355	3.885	4.544	3.886	2.356	
10	2.426								
	2.353	3.896							
	3.868	2.427	3.859						
	3.857	3.895	2.416	2.354					
	2.353	2.316	2.442	2.353	2.441				
	2.363	2.305	2.536	2.363	2.536	2.530			
	3.878	4.645	2.358	3.879	2.359	3.893	2.403		
	2.391	3.966	2.323	4.575	3.860	3.868	2.274	2.419	
	4.575	3.968	3.859	2.392	2.323	3.867	2.273	2.417	3.932

theory. For further reading on the OPBE performance in the prediction of the correct spin states of iron complexes the reader is forwarded to [19]. The next section briefly reviews

the methodology, the third section shows the results of our ab initio calculations and the final section discusses the conclusions.

# Methods

Calculations are performed in the framework of DFT using the Gaussian-09 program [20]. We choose the OPBE functional, which is a combination of the Handy's OPTX modification of the Becke's exchange functional [21, 22], and the gradient-corrected correlation functional of Perdew, Burke and Ernzerhof of (PBE) [23, 24]. The basis set used is the triple- $\zeta$  valence (TZV) basis set also known as {842111/631/411} [25]. Our earlier work using DFT has produced acceptable results when compared to available experimental data [26–45].

All of the structures are initially optimized using quadratic convergence with a threshold of  $10^{-6}$  for the selfconsistent field (SCF) wavefunction due to the difficulty to reach convergence with the default settings. The initially optimized structures and wavefunctions are finally used as inputs to optimize them with the default threshold of  $10^{-8}$ .

All of the geometry optimizations are carried out with the Berny algorithm using the geometry-optimization energyrepresented direct inversion in the iterative subspace (GEDIIS) algorithm, which is implemented by default in Gaussian-09.

We do not impose any symmetry constraints; however, calculations are restricted to collinear arrangement of magnetic moments. The convergence criteria are the default values in the program,  $4.5 \times 10^{-4}$  a.u. and  $1.8 \times 10^{-4}$  Å for the maximum force and displacement, respectively.

In our spin-polarized calculations, unpaired spin populations are obtained by a Mulliken population analysis. Energies of the optimized structures are reported here, including the zero-point energy (ZPE) correction. The optimized structures are verified as local minima by finding no imaginary frequencies.

In addition, we analyze the stability and electronic properties of iron clusters based on size evolution of the magnetic moment per atom, binding energy per atom, the dissociation energy, the first vertical and adiabatic ionization energy and electronic affinity. The average binding energy per atom is defined as

$$E_b(n) = [E_n - nE_1]/n$$
(1)

and the dissociation energy is computed from

$$D_e(n) = (E_{n-1} + E_1) - E_n = (n-1)E_b(n-1) - nE_b(n), \quad (2)$$

where  $E_n$  is the total energy of  $\text{Fe}_{n=2-10}$  including the ZPE correction.



**Fig. 2** Fe<sub>n</sub> (n=2-10) ground states. Our calculated binding energies are the smallest among other reports. Our calculated dimer value of -0.62 eV/atom is the closest to the experimental value of -0.57 eV/atom

The ionization energy (IE) and electron affinity (EA) are defined as

$$IE = E(Fe_n^+) - E(Fe_n) \tag{3}$$

and

$$EA = E_n(Fe_n) - E(Fe_n^{-}), \tag{4}$$

respectively. Where  $E(Fe_n^+)$ ,  $E(Fe_n^-)$  and  $E(Fe_n)$  are the total energies of the cation, anion, and neutral clusters, respectively, all of which are calculated at the optimized geometries of the neutral cluster for the vertical calculations, and at their corresponding relaxed geometries for the adiabatic cases.

<b>Table 2</b> Bond distance $(d_o)$ ,		
frequency $(\omega_o)$ and bond disso-		$d_o(A)$
ciation energy $(D_e)$ for the iron		
dimer	Experimental	2.0
	Multiplicity (M)	7

	$d_o(\text{\AA})$	$d_o( m \AA)$		$\omega_o(\mathrm{cm}^{-1})$		$D_e(eV)$	
Experimental	2.02±0.0	2 [51]	299.6 [66	]	1.14 eV±0	.10 eV [60]	
Multiplicity (M)	7	9	7	9	7	9	
OPBE/TZV	2.00	2.16	397.9	309.5	1.24	1.16	

In order to analyze stability, the chemical hardness [46–48] is defined in the framework of DFT as the second derivative of the total energy  $E_n$  with respect to the number of electrons, n, at a fixed external potential v(r). According to DFT, it is also the second derivative of the electronic energy with respect to the number of electrons, n, when the external potential, v(r) is kept fixed:

$$\eta = \frac{1}{2} \left( \frac{\partial^2 E_n}{\partial n^2} \right)_{\nu(r)} = \frac{1}{2} \left( \frac{\partial \mu}{\partial n} \right)_{\nu(r)} \approx \frac{I - A}{2}, \tag{5}$$

where  $\mu$  is the chemical potential; *I* and *A* are the vertical IE and EA, respectively, from a finite difference approximation; then, using Koopmans's theorem, we can approximate hardness as:

$$\eta \approx \frac{1}{2} (\epsilon_{LUMO} - \epsilon_{HOMO}), \qquad (6)$$

where the difference  $\epsilon_{LUMO} - \epsilon_{HOMO}$  is the energy gap between the unoccupied and occupied orbitals [49].

## **Results and discussion**

The ground state neutral clusters and their pair distances are shown in Fig. 1 and Table 1, respectively. In general, the optimized geometries and magnetic moments of the ground states are similar to previous reports [10, 11, 13, 16, 50]. The ground states and isomers from the Fe<sub>3</sub> to the Fe<sub>10</sub> clusters are distorted from the symmetrical forms because of the Jahn-Teller effect. According to the Jahn-Teller theorem, if the

highest occupied molecular orbital (HOMO) of a non-linear molecule in a symmetrical conformation is not fully occupied, asymmetrical structural distortions (Jahn-Teller effect) occur to remove the degeneracy.

Energetic and structural analysis of clusters  $Fe_{2-10}$ : ground states and isomers

The septet and nonet spin states of the dimer are only separated by 81.54 meV, with the septet as the lowest energy state and yielding the closest bond length of 2.003 Å to the experimental value of 2.02 Å [51]. This is also in good agreement with previous computational studies [7, 52–55] that consider the septet as ground state. However, an experiment performed by Leopold et al. [56, 57] suggested the  ${}^9\Sigma_g$  as the ground state. Thus, predicting the dimer as being a septet is not conclusive because both the septet and nonet have similar probabilities to be found in experiments and also because we find the vibrational frequency of the nonet to be the closest to the reported experimental value. These results are summarized in Table 2.

The potential energy surface of the Fe trimer has several local minima [58]; therefore, several optimized structures are possible for the ground state. We find that the Fe<sub>3</sub> ground state is approximately an isosceles triangle of 2.17 Å base and 2.28 Å legs with M=11, in agreement with [11, 52, 59]. While a possible isomer could have a linear geometry with the same multiplicity, other multiplicities with linear geometries show imaginary frequencies.

Fig. 3 The infrared spectrum is shown for Fe<sub>n</sub> (n=3-10). In the case of Fe<sub>3</sub> we obtained a strong peak at 103 cm<sup>-1</sup>, and two very small peaks at 241 cm<sup>-1</sup> and 350 cm<sup>-1</sup>. Strong peaks indicate antisymmetrical stretching modes





Fig. 4 Ionization energy and electron affinity (adiabatic and vertical) for Fe<sub>n</sub> (n=2-10)

The ground state of the tetramer is a distorted tetrahedron **4a** of  $D_{2d}$  symmetry with four short 2.24 Å and two long 2.57 Å bond lengths, in excellent agreement with the non-collinear GGA pseudopotential approach reported by Hobbs et al. [14].

Our calculations find a distorted trigonal bipyramid 5a as the ground state, with minimum bond length of 2.26 Å. A

second isomer is the  $C_{2v}$  planar structure **5b**. The Fe<sub>5</sub> isomers are stable with  $3.2\mu_B/atom$ .

Despite the increased number of isomers, the octahedron is found to be the ground state of the hexamer. There are two predicted octahedral forms (**6a** and **6b**) which are separated by 7.09 meV. **6a** has a square base of side 2.55 Å and the separation between the top and bottom atoms is 2.8 Å. The second isomer **6b** has a rectangle base of sides 2.72 Å and 2.31 Å, whose maximum inter-atomic distance is 2.95 Å. All the hexamer structures have the same multiplicity of 21.

A distorted pentagonal bipyramid-like structure **7a** is the ground state, followed by the capped octahedron ( $C_{3v}$ ) isomer **7b**. Their energy difference is about 0.31 eV. However, results from Ma et al. [11] and Yu et al. [50] showed a regular pentagonal bipyramid ( $D_{5h}$ ) 21.48 meV and 1.13 eV below the  $C_{3v}$  structure, respectively.

For the Fe<sub>8</sub> cluster, the bidisphenoid structure ( $D_{2d}$ ) is the lowest in energy with a magnetic moment of  $3\mu_B/atom$ . A structure with similar energy (0.75 eV) is the bicapped octahedron **8b**, which is in the same isomer order as in Yu et al. [50] (0.59 eV). The capped pentagonal bipyramid converge without symmetry constraints to our ground state **8a**. Another isomer structure ( $D_2$ ) is found at 1.29 meV higher in total energy by Ma et al. [11]; however, the  $D_2$  geometry showed a convergence to our bidisphenoid structure. Our third isomer is characterized by a distorted hexagonal bipyramid **8c**.

The first three Fe<sub>9</sub> isomers are in good agreement with Ma et al. [11]. However, the order for the first two isomers (a regular bicapped pentagonal bipyramid **9a** and an irregular tricapped trigonal prism structure **9b**) were not the same as shown for the first two isomers in Kohler et al. [10] and Diéguez et al. [13]. Also, Rollmann et al. [12] found our third isomer **9c** as their ground state.

The Fe<sub>10</sub> lowest energy structure **10a** is a  $C_{3v}$  symmetry group of multiplicity 31; however, this structure was referred [10, 13] to as the second isomer with M=29. A D<sub>4d</sub> structure **10b** with a multiplicity of 29 is predicted as the second isomer; to some extent, Ma et al. [11] found such a structure as the ground state, but with M=31. A D<sub>2h</sub> geometry **10c** with M=31 is predicted as the third isomer.

п	$E_n$ (Ha)	$HLG_{\alpha}\left( eV\right)$	$HLG_{\beta}\left( eV\right)$	IE (eV)	EA (eV)	η (eV)
2	-2527.85780	1.22	0.36	5.81	0.07	2.87
3	-3791.82392	0.22	0.54	5.15	0.75	2.20
4	-5055,81431	0.58	0.60	5.43	1.11	2.16
5	-6319,82017	0.39	0.55	5.42	1.38	2.02
6	-7583.83977	2.00	0.52	5.79	1.22	2.28
7	-8847.85368	1.76	0.39	5.41	1.00	2.20
8	-10111,85532	1.92	0.54	5.20	0.92	2.14
9	-11375.84750	1.28	0.51	4.66	1.01	1.82
10	-12639,84878	0.15	0.51	4.26	1.39	1.44

**Table 3** Total energy including ZPE ( $E_n$ ), HOMO-LUMO gap for alpha and beta electrons (HLG<sub> $\alpha$ </sub> and HLG<sub> $\beta$ </sub>), vertical ionization energy (IE), electron affinity (EA) and chemical hardness ( $\eta$ ) for the Fe<sub>n</sub> clusters

Dissociation energy and binding energy analysis of clusters  $Fe_{2-10}$ 

In the case of the iron dimer dissociation energy, the error is 0.1 eV comparing the present computational value of 1.24 eV and the experimental value of  $1.14\pm0.10$  eV [60] (-0.57 eV/ atom for the binding energy,  $E_b(n=2)=-D_e(n=2)/2$ ). In general, the dissociation energy (Fig. 2a) follows a growing behavior up to the Fe<sub>6</sub> cluster, meaning it is the most stable structure in our domain of analysis. The Fe<sub>3</sub> dissociation energy necessary to form Fe<sub>2</sub> and Fe is 1.63 eV in contrast with the experimental value of 1.82±0.13 eV [60]. The maximum error of 0.63 eV (Fe<sub>5</sub>) and the overestimated values can be explained because of the mixture of electronic states in the iron clusters, as well as geometries, in the experiment. Figure 2a only considered the ground states and not the isomers. The dissociation energy of the planar 5b is about 1.89 eV in contrast with the experimental value of  $2.08\pm0.24$  eV. The Fe<sub>8</sub> isomers are 1.85 eV (8b) and 1.49 eV (8c) in contrast with the experimental value of 2.12±0.27 eV. This suggests the important role of multiplicities and geometries in the experiment, i.e. the experimental dissociation energy is an average of the isomers. This explanation fails for both Fe3 and Fe9.

The decay behavior of the binding energy curve (Fig. 2b) means that the neutral structures are stable. These values are in favor of being the smallest among other computational methods: LDA+U [61], DFTB [10], BPW91/LANL2DZ [50], BLYP/DNP [11], LSDA [12] and non collinear LSDA [9].

Spectroscopy analysis of clusters Fe<sub>2-10</sub>

The IR vibrational spectra of the ground states are shown in Fig. 3. For the Fe<sub>3</sub>, we obtain a strong peak (antisymmetric mode) at 102.6 cm<sup>-1</sup> and two weak peaks (symmetrical mode) at 241 cm<sup>-1</sup> and 350 cm<sup>-1</sup>. The assignment of the



**Fig. 5** Size evolution of the magnetic moment ( $\mu_B$ /atom) for our Fe<sub>n</sub> (n= 2-10) ground states compared with previous computational methods

symmetrical stretching mode at 241 cm<sup>-1</sup> is given by considering the vibrational frequency of the Fe<sub>2</sub> nonet state (309.5 cm<sup>-1</sup>). This mode also corresponds with the one found by Haslett et al. at 249 cm<sup>-1</sup>. Moreover the mode at 102.6 cm<sup>-1</sup> corresponds with the antisymmetric stretching mode at 180 cm<sup>-1</sup> found by Nour et al. [62].

Ionization potential, electro affinity, and HOMO-LUMO relations

We calculate adiabatic and vertical IE and EA for the Fe<sub>2-10</sub> ground states. Adiabatic energies are obtained by the optimization of several structures and multiplicities, whereas for the vertical transitions calculations both energies are computed at the equilibrium geometries of the neutral clusters. ZPE corrections are taken into account for both vertical and adiabatic values. Figure 4 summarizes IE and EA results, where other high level theoretical [52, 55, 63] and experimental data [56, 64, 65] are shown. We show the adiabatic results from Castro and Salahub [55] and the adiabatic results from Chrétien and Salahub [52]. Vertical values are from Gong and Zheng [63].

All vertical and adiabatic multiplicities (for anion and cation) are the same except for those of Fe<sub>6</sub> that have multiplicities of 20 and 22 for the vertical and adiabatic cationic cluster, respectively. Moreover, all the relaxed ionic forms tend to have a similar like-structure as the isomer they originate from, except for the Fe<sub>6</sub> which in both adiabatic anionic and cationic prefers the **6b**-like structure. Considering the ZPE correction, the IE and EA values have increased and decreased, respectively, by values less than 0.31 eV in the Fe<sub>10</sub> case.

Both adiabatic and vertical values are underestimated compared with experimental data. In general, the error is no larger than 1.02 eV in the case of EA and 1.10 eV in IE, except for the adiabatic and vertical  $\text{Fe}_3^+$ , adiabatic  $\text{Fe}_4^+$  and vertical  $\text{Fe}_{10}^+$ where the error is with errors less than 1.31 eV compared to the experiment [64]. The most accurate result is for the Fe<sub>6</sub> anion

Table 4 Magnetic moments for the adiabatic ions ( $\mu_B$ /atom)

n	Cation ( $\mu_B$ /atom)	Neutral ( $\mu_B$ /atom)	Anion ( $\mu_B$ /atom)
2	3.50	3.00	3.50
3	3.00	3.33	3.67
4	2.75	3.50	3.75
5	3.00	3.20	3.40
6	3.50	3.33	3.17
7	3.29	3.14	3.00
8	3.13	3.00	2.88
9	3.00	2.89	3.00
10	2.90	3.00	3.10

and cation, with errors less than 0.41 eV. In addition, the IE and EA of the adiabatic  $Fe_6$  and  $Fe_5$  are the highest ( $Fe_6$  is second in the vertical IE case, after the dimer) in the whole range of analysis, indicating that the hexamer needs more energy to remove one electron and that the pentamer is more stable by releasing energy when adding one electron.

As suggested by the chemical hardness in Table 3, the iron dimer ( $\eta$ ) is the most stable theoretically, followed by the hexamer. Adding a third atom to the dimer, increases the interatomic distances (Table 2) and reduces the bond strength and dissociation energy (Fig. 2a). This trend continues up to Fe<sub>6</sub>, which shows a high value of  $\eta$ , predicting high stability. Local maxima values of  $\eta$  are found in Fe<sub>6</sub>, Fe<sub>7</sub> and Fe<sub>3</sub>, which are the second, third and fourth most stable clusters, respectively. However, the HLG shows a different stability order (tetramer, octamer, hexamer). Roy et al. [16] found the octamer, followed by the hexamer and tetramer, as the most stable structure from the HLG analysis.

Magnetic moment and adiabatic ionic magnetic moments of Fe<sub>2-10</sub> clusters

The results for the magnetic moment per atom of the neutral clusters are compared with other theoretical calculations in Fig. 5.

For the Fe<sub>4</sub> cluster, the magnetic moment per atom yields its maximum of  $3.5\mu_B$  which is the same as the one found with a GGA ultrasoft pseudopotential procedure performed by Šljivančanin et al. [8]. In the case of Fe<sub>6</sub>, a  $3.33 \mu_B$ /atom is found in agreement with other DFT based calculations: GGA [7, 8, 11, 12, 14, 50], LDA [13, 15] and DFTB [10] studies. All the Fe<sub>9</sub> isomers have a total magnetic moment of 26  $\mu_B$ . In the case of the Fe<sub>10</sub> isomers, all the structures but **10b** (28  $\mu_B$ ) have a magnetic moment of 30  $\mu_B$ .

Table 4 shows the adiabatic ionic magnetic moments. The common pattern is the convergence of the ion magnetic moments to the neutral values, where the highest magnetic moments are from the Fe<sub>3</sub><sup>-</sup> and Fe<sub>4</sub><sup>-</sup> clusters. Among cations only, Fe<sub>2</sub><sup>+</sup> and Fe<sub>6</sub><sup>+</sup> have the highest magnetic moment per atom, indicating a great number of unpaired electrons, in spite of the fact that the adiabatic cation shows the highest IE. The low total magnetic moment of  $11\mu_B$  for Fe<sub>4</sub><sup>+</sup> [7] and its regular tetrahedral structure are corroborated in the present work.

## Conclusions

An acceptable performance of the all-electron OPBE/TZV model for searching ground states and their low-lying isomers is obtained for small iron clusters up to ten atoms. Geometrical structures of the neutral clusters are in good agreement with previous computational studies, but a

different order in the isomers is obtained for  $Fe_8$ ,  $Fe_9$  and  $Fe_{10}$ . This could be because, for a ground state cluster, some geometries are more energetically favored by different levels of theory. Distortions are in agreement with the Jahn-Teller effect.

Furthermore, multiplicities are accurately predicted, yielding magnetic moments around 3  $\mu_B$ . In the case of the Fe<sub>2</sub>, two closest low lying spin states are found: the septet and the nonet. Both states are predicted to have a similar probability to be formed; however, the nonet is the state that has the correct vibrational frequency of 299.6 cm<sup>-1</sup>. This result in the dimer is also supported by the direction that the dissociation energy curve follows.

Our reported binding energy of the dimer is the closest to the only experimental value available; and all the cluster energies are the smallest among those from other level of theoretical studies. Furthermore, the decay behavior of the binding energy curve suggests that our reported cluster structures are the ground states.

Compared with the experimental data, all our IE and EA results are underestimated. The  $Fe_6$  cluster corresponds to the most stable structure in the hardness analysis and shows the highest IE in the range from three to ten iron atoms. Furthermore, the dissociation energy is the highest indicating the most energetically stable cluster.

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